

# NUMFabric: Fast and Flexible Bandwidth Allocation in Datacenters

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# Datacenter fabric proposals

A word cloud of datacenter fabric proposals. The words are arranged in a roughly rectangular shape, with varying sizes and colors. The colors include shades of green, brown, blue, and gold. The words are: D2TCP, DIBS, Fastpass, CONGA, MPTCP, FastLane, Presto, Quartz, RepFlow, MCP, DCTCP, pFabric, D-CUBE, PQ, and HULL.

D2TCP DIBS Fastpass CONGA  
MPTCP FastLane Presto Quartz  
RepFlow MCP DCTCP pFabric D-CUBE  
PQ HULL

Which one does the operator pick?



D2TCP DIBS Fastpass CONGA  
MPTCP FastLane Presto Quartz  
RepFlow MCP DCTCP pFabric D-CUBE  
ADQ HULL

Is there a single fabric that provides flexible and fast bandwidth allocation control?

Yes ! NUMFabric provides a **flexible** fabric that is also **fast**.

# Flexible and Fast

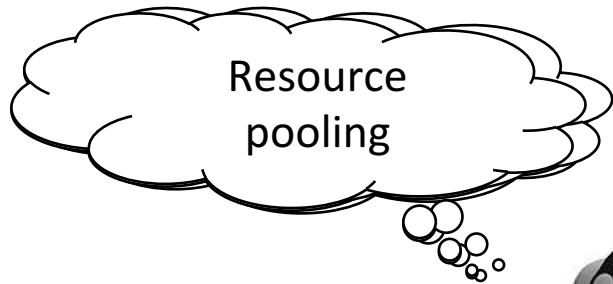
## Flexible

- Supports wide variety of bandwidth allocation objectives

## Fast

- Flows converge to correct rates before the datacenter workload changes

# NUMFabric: Flexibility



Translate to utility functions



$$\text{maximize } \sum_i \sum_{l \in S_i} w_i x_i^l * \log(y_i)$$

where  $y_i$  = aggregate rate of flow across all subpaths

Flow  $i$ 's utility at rate  $x_i$

send utility function to hosts



- $x_i$  ← rate of flow  $i$
- $s_i$  ← size of flow  $i$
- $w_i$  ← weight of flow  $i$

# Network Utility Maximization in general

$$\textit{maximize } U(X) = \sum_{i \in S} U_i(x_i)$$

*subject to*

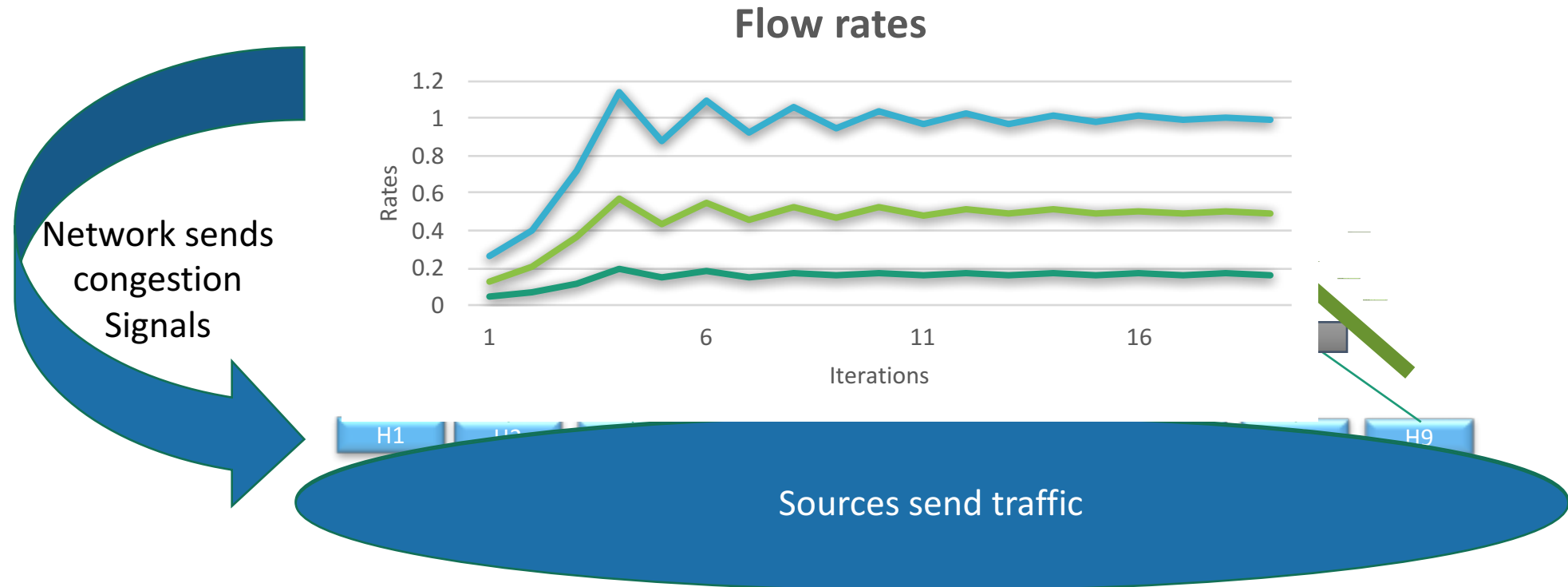
$$AX \leq C$$

$$X \geq 0$$

Problem ?

Existing NUM solutions are slow and unsuitable for data center workloads

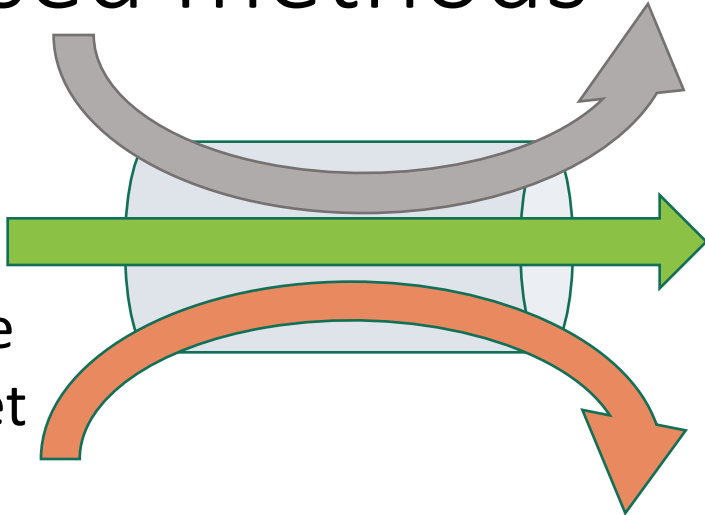
# Existing distributed NUM solutions



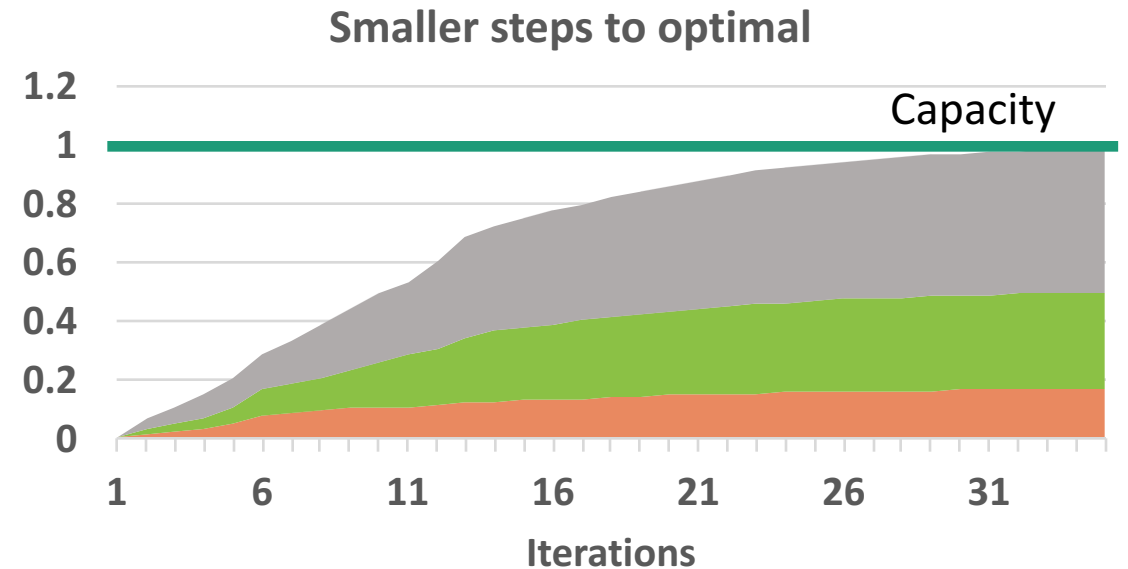
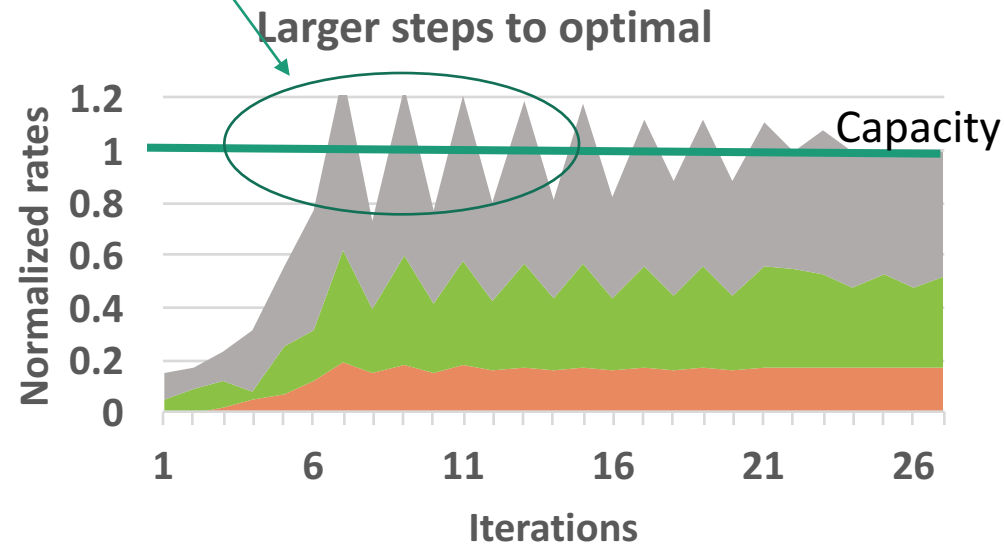
- Each source iteratively adjusts rates following its own gradient towards optimal
- The sum of the rates moves towards the global optimal



# Gradient based methods

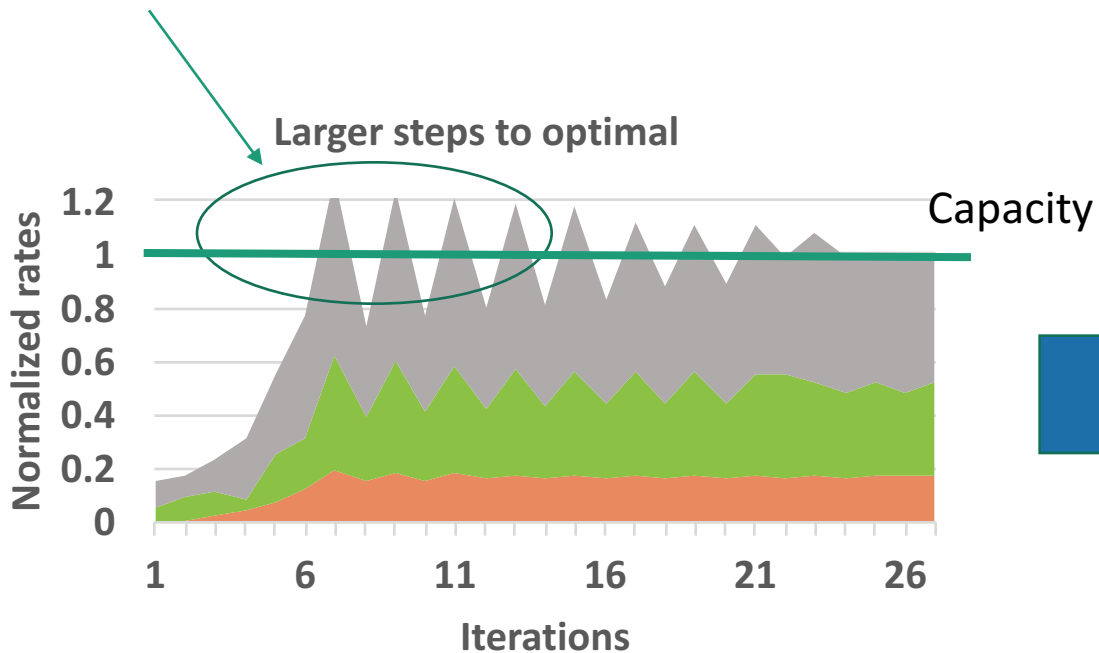


Overshooting might cause bloated queues and packet drops



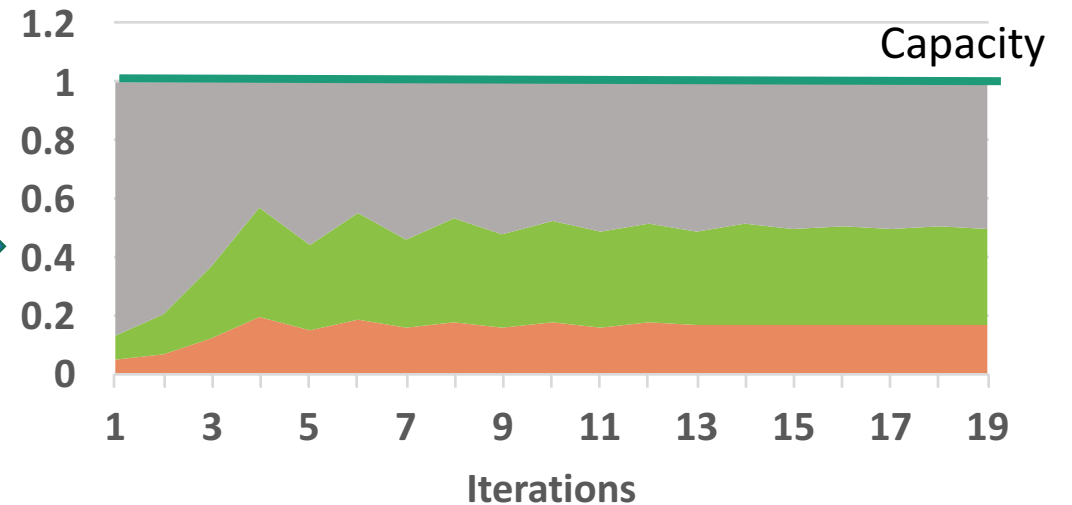
# How can we fix this?

Overshooting might cause drops, queues bloating



Can we enable larger steps to optimal but without over-shooting and under-utilization?

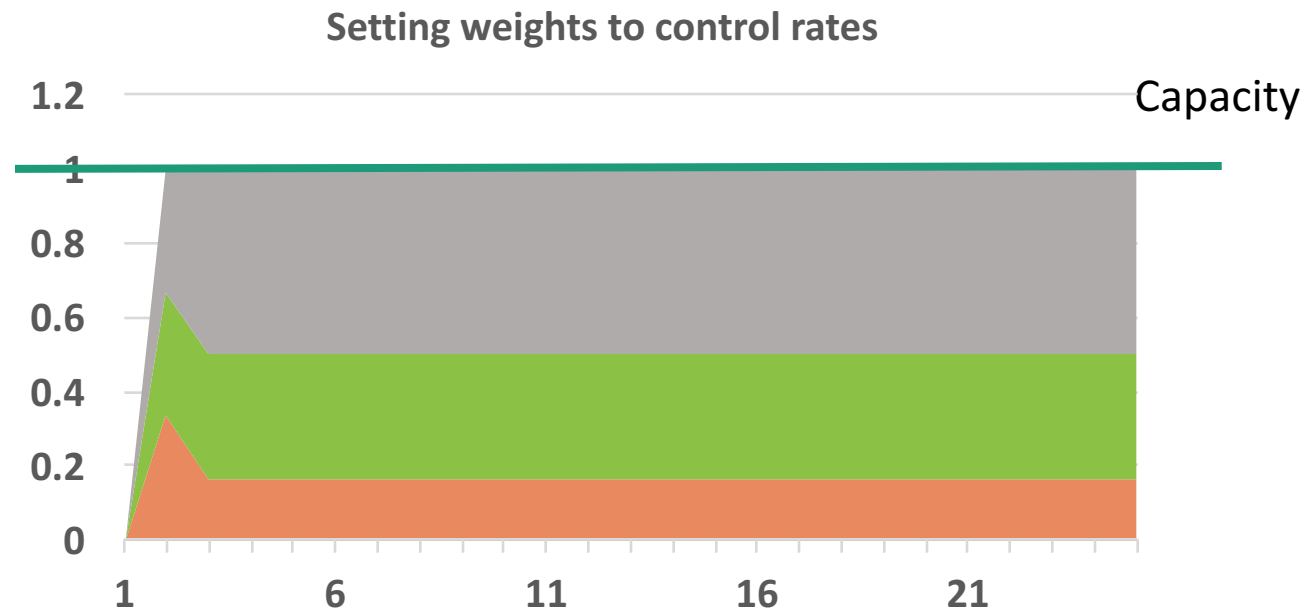
Larger steps to optimal



Use Weights instead of rates !  
Setting weights of the flow and allowing a fabric to allocate rates proportional to the weights enables exactly this.

# NUMFabric key idea

- In NUMFabric, sources give up direct control over rates
- The sources specify “weights” and the Weighted Max-Min fabric allocates relative rates proportional to the weights of all flows



Application level objective

Translate to utility functions



$$\text{maximize } \sum_i U_i(x_i)$$

Flexible



Layer that sets weights of flows based on network feedback

Weighted Max-Min rate allocation according to the weights



Fast

Weight inference

# Distributed NUM mechanism

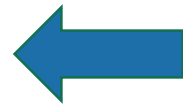
NUM Objective

$$\text{Maximize } \sum_i U_i(x_i)$$

KKT Conditions: Equations that must necessarily be true at optimal solution

Price of a link : variable that indicates the congestion level at the switch

$$p_l \left( \sum_{i \in S(l)} x_i - c_l \right) = 0$$



At optimal, either the link is fully utilized or the price of the link is zero

$$U_i'(x_i) = \sum_{l \in L(i)} p_l$$



At optimal, the marginal utility of the source is equal to the sum of the prices along the path of the flow

# Distributed NUM mechanism

Switches set their prices measuring congestion

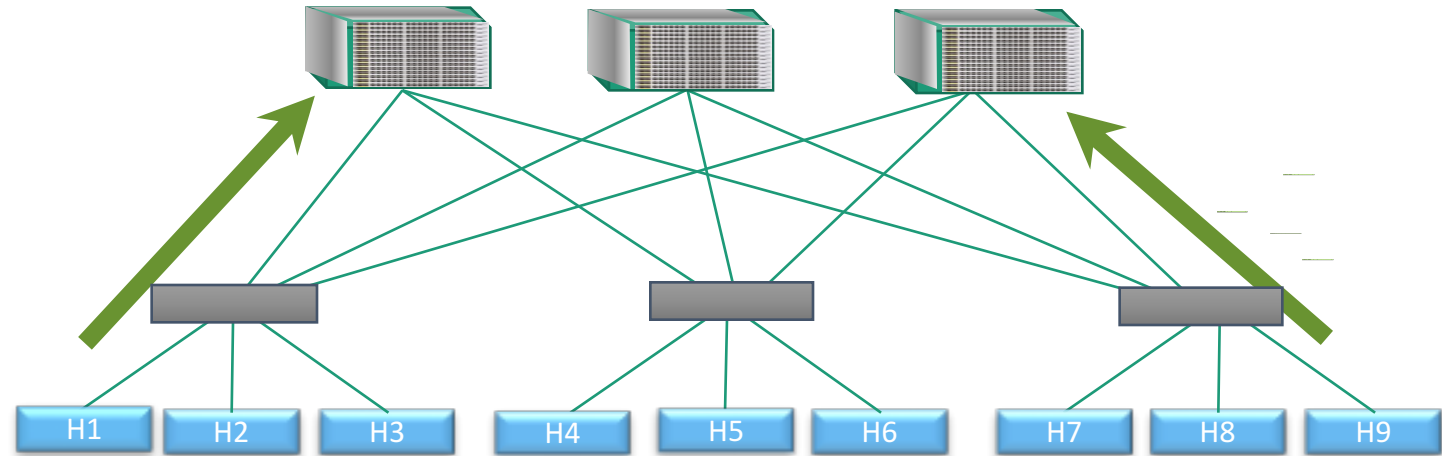
$$p_l(\sum_{i \in S(l)} x_i - c_l) = 0$$

solve

$$p_l = p_l + \alpha * (\sum_{i \in S(l)} x_i - c_l)$$

$$\sum_{l \in L(i)} p_l$$

Network congestion signals



Sources adapt rates of flows

Sources set the rates of the flows using price feedback

$$U_i'(x_i) = \sum_{l \in L(i)} p_l$$

solve

$$x_i = \text{Inverse of } U_i'(\sum_{l \in L(i)} p_l)$$

# NUMFabric iterations

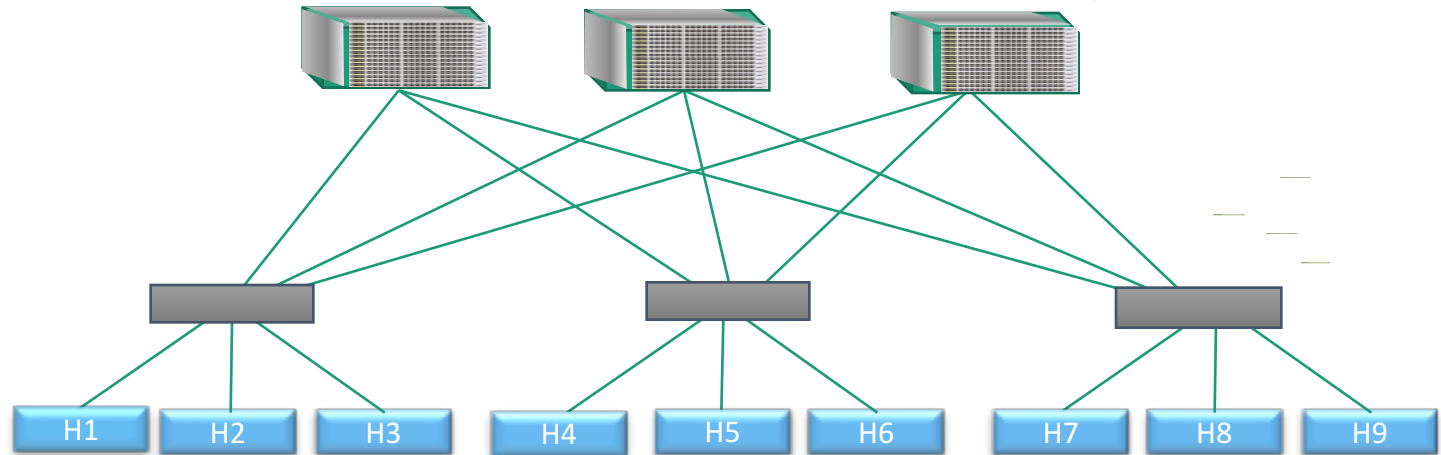
Controlling rates directly causes the brittleness in the existing solutions.

$$p_l(\sum_{i \in S(l)} x_i - c_l) = 0$$



WMM layer  
always achieves  
100% link  
utilization

Switches adapt prices at every iteration so that the flow rates move closer to optimal



$$U_i'(x_i) = \sum_{l \in L(i)} p_l$$



$$w_i = \text{Inverse of } U_i'(\sum_{l \in L(i)} p_l)$$

WMM layer converts these weights to rates

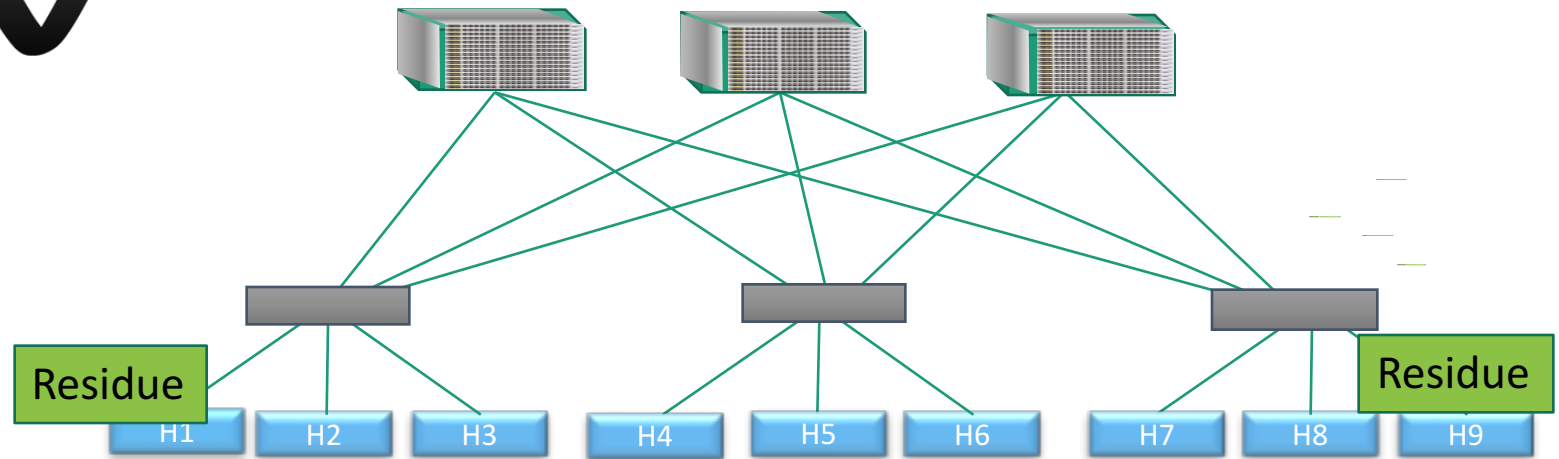


# NUMFabric iterations

As we know, controlling rates directly causes the brittleness in the existing solutions.

$$p_l(\sum_{i \in S(l)} x_i - c_l) = 0 \quad \checkmark$$

Switch  $p_l = p_l + \min\left(\frac{\text{residue}_i}{\text{hops traversed by flow}_i}\right)$  that the

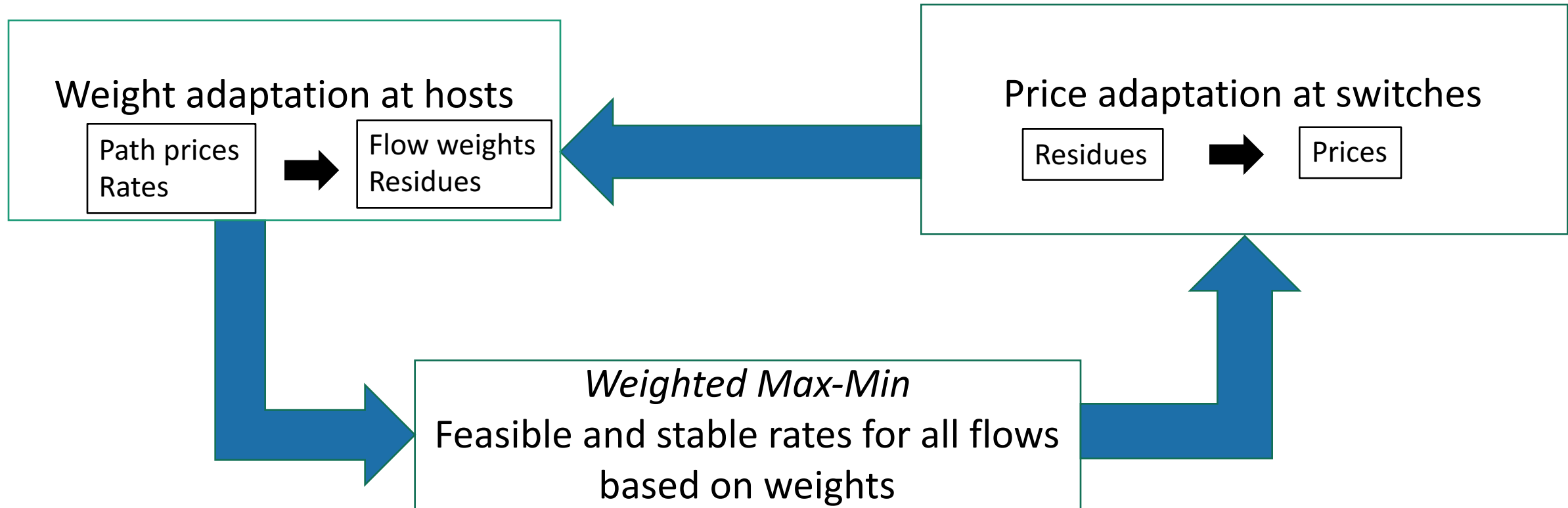


$$U_i'(x_i) = \sum_{l \in L(i)} p_l$$



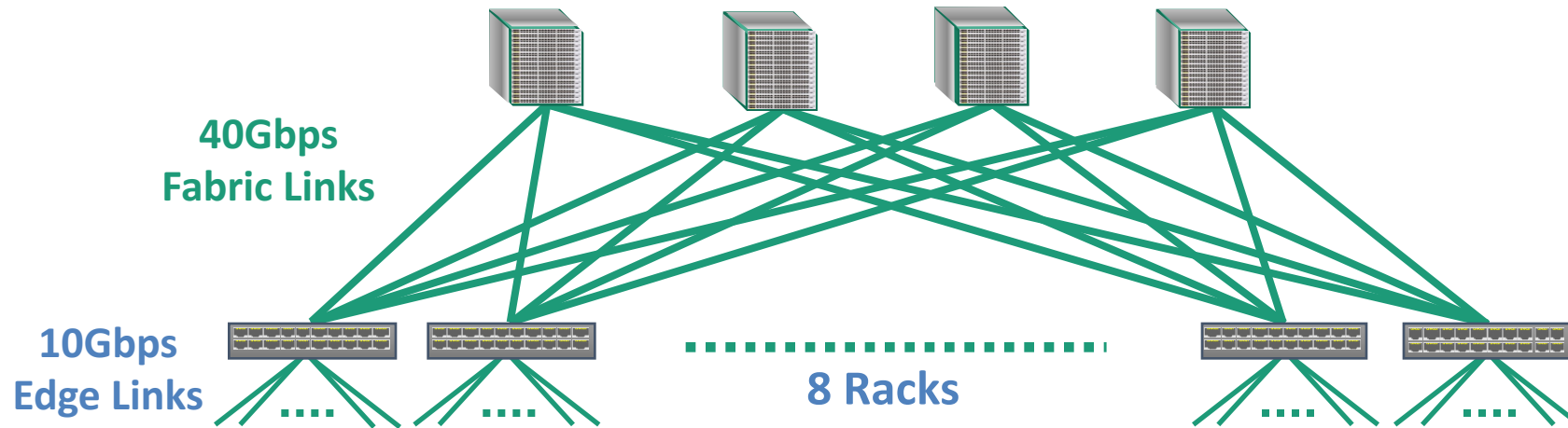
$$\text{Residue} = U_i'(x_i) - \sum_{l \in L(i)} p_l$$

# Operation summary



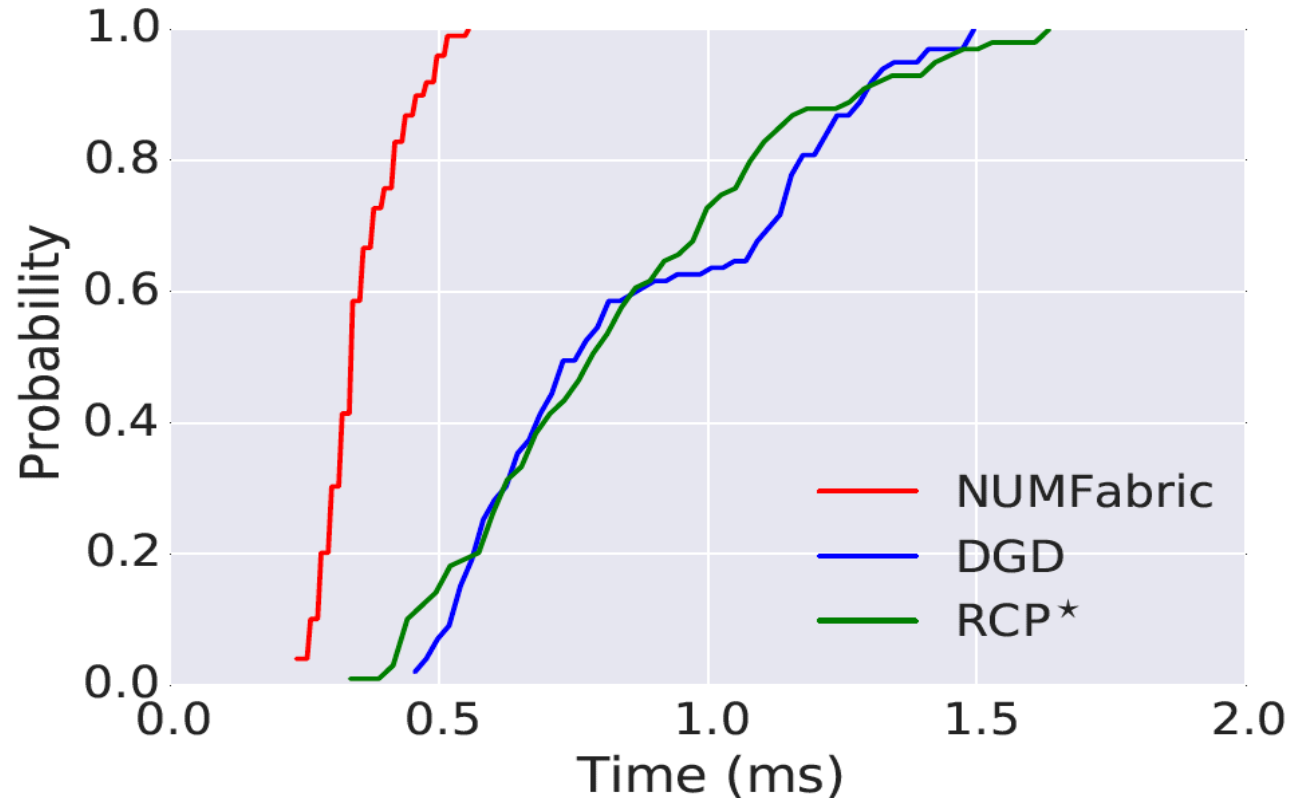
Evaluation

# Evaluation setup



- ns3 simulations: 128-port leaf-spine fabric
  - RTT =  $\sim 16\mu\text{s}$
- Evaluate speed of convergence
- Evaluate flexibility
  - Compare the bandwidth allocations on NUMFabric with different utility functions against point solutions for different objectives— pFabric, MPTCP, etc.

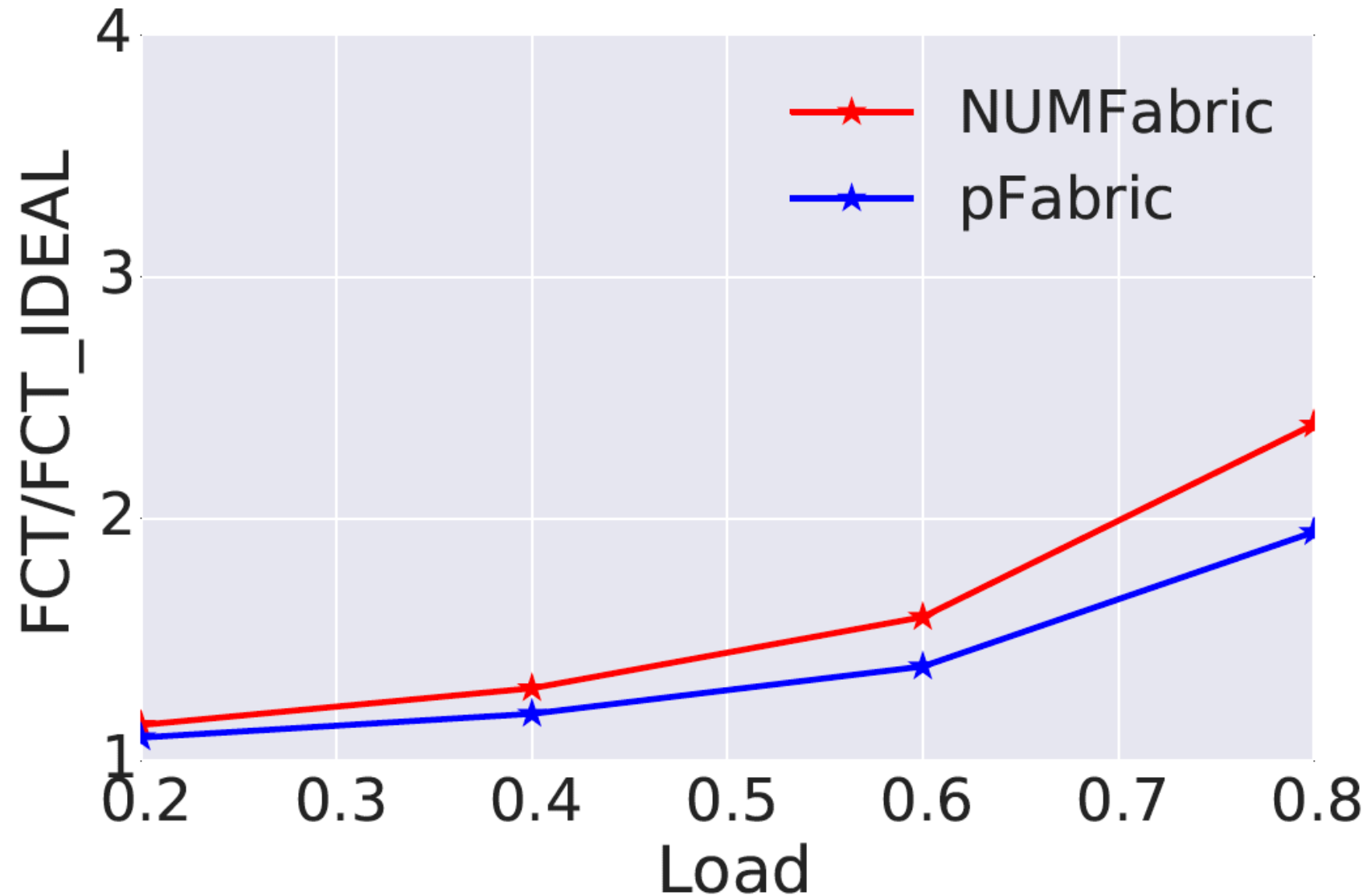
# Fast convergence



DGD : Dual Gradient Descent algorithm  
RCP\* : Alpha-Fair RCP

- 100 flows start/stop at every “event”.
- We let the system converge before triggering another event
- Median convergence time (335 us) of NUMFabric is 2.3X better than the other algorithms

# Flexibility : minimize flow completion times

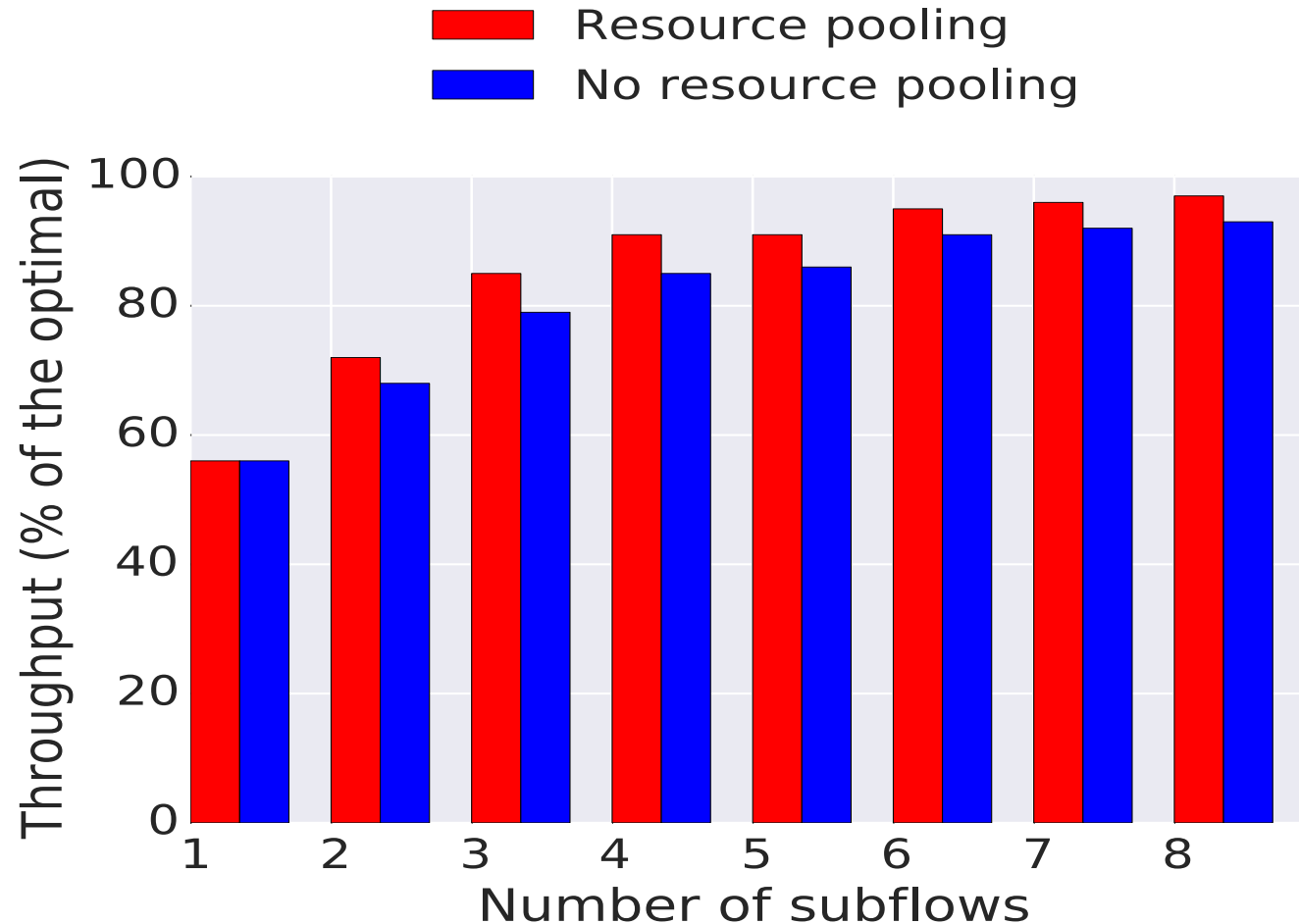


$$\text{maximize } \sum_i \frac{x_i}{s_i}$$

$x_i \rightarrow$  rate of the flow

$s_i \rightarrow$  size of the flow

# Flexibility : minimize flow completion times



$$\textit{maximize } \sum_i \log(y_i)$$

where  $y_i$  = aggregate rate of flow across all sub-paths

# Conclusions

- NUMFabric enables operators to **flexibly optimize** network's bandwidth allocation for different bandwidth allocation objectives
- NUMFabric uses weights as knobs to influence rates and thus, decouples the objectives of finding optimal rates and stable rates. This makes it **2-3X faster existing mechanisms**.
- Using NUMFabric with objective functions on co-flows, VM-level and tenant-level aggregates is focus of our current and future work.



Thank you